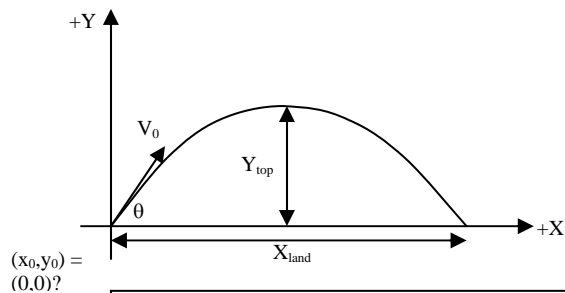


## Two Dimensional Motion

### PROCEDURE:

1. Draw a neat sketch showing entire path of each projectile, and clearly label **Initial** and all other points of interest.
2. Pick a coordinate system. Label **ORIGIN** and **+X, +Y- direction** . Since the projectile equations give the position, not distance traveled, this is a very important step. If you have two or more projectiles, the equations for each must use the same reference point (ORIGIN).
3. Resolve the initial velocity into X, Y- components (whether known or unknown). For some problems, you may want to skip this step.
4. Write the equation for the **Horizontal position** and then copy it below with all the known initial values substituted in.
5. Write the equation for the **Vertical position** with all the known initial values substituted in. Also write the equation for the vertical **velocity**, if necessary.
6. If there is more than one projectile, repeat steps 3 through 5 for each projectile.
7. Write down known facts (position, velocity, time, etc.) about the points of interest, such as "The object is at  $y = 0$  when it lands."
8. Solve for unknown quantity or quantities.



#### Potentially Useful Equations

$$V_{x,0} = V_0 \cos(\theta)$$

$$V_{y,0} = V_0 \sin(\theta)$$

$$x_1 = x_0 + V_{0,x} (t_1 - t_0) + \frac{1}{2} a_x (t_1 - t_0)^2$$

(usually  $t_0$  and  $a_x$  are 0)

$$y_1 = y_0 + V_{y,0} (t_1 - t_0) + \frac{1}{2} a_y (t_1 - t_0)^2$$

(usually  $t_0=0$  and  $a_y = -g$ )

$$V_{y,1} = V_{1,y} + a_y (t_1 - t_0)$$

$$V_{y,1}^2 = V_{y,0}^2 + 2 a_y (y_1 - y_0)$$

For the diagram above find the following: [see also 3.62]

A) Find the maximum height. B) How much time to get to this height?

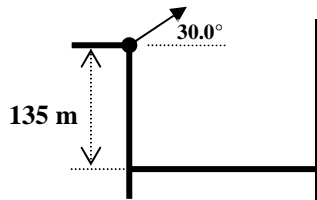
A baseball is hit from the ground with an initial speed of 40.2 m/s at an angle of  $36.87^\circ$ . A player, initially 120.7 m away, starts running towards the ball at his top speed of 7.61 m/s. Will he catch the ball? Assume the ball starts 1.00 meters above ground and the player can dive if necessary.

For the diagram above find the following: [see also 3.62]

- A) Find the location where the ball lands on the ground,
- B) the time of flight
- C) the angle that maximizes the horizontal distance
- D) the special condition for this maximum angle.
- E) For what other launch angle does the ball land at the same place as it did in part (A)?

A projectile is fired from the edge of a cliff, 135 m high, with a velocity of 60.0 m/s at an angle of  $30.0^\circ$ . [see also 3.24] Find:

- A) the horizontal range (distance),
- B) the time to impact,
- C) the x and y velocity components at impact
- D) the speed and direction of motion at impact



3.46 (similar to 3.58) A stone is kicked so that it leaves the ground with an initial velocity of 10.0 m/s at an angle of  $37.0^\circ$ . The stone is kicked towards a platform whose near edge is 3.00m away and 1.00 m high.

- (a) What are the components of the stone's initial velocity?
- (b) How high does it go?
- (c) How far from the "near edge" does it land on the platform?
- (d) How fast is it moving just before it hits the platform?